

# Tampines Secondary School

## Sec 4 Prelim Math Paper 2 2024 Marking Scheme

Total Marks: 90

✓ = follow through

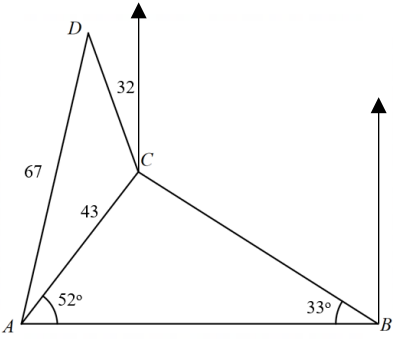
No.	Answers	Marks
1a	$\frac{6(a+1)^3}{7b} \times \frac{28b}{9(a+1)}$ $= \frac{2(a+1)^2}{1} \times \frac{4}{3}$ $= \frac{8(a+1)^2}{3}$	<p>B1 (for <math>(a+1)^2</math> seen)</p> <p>B1 (for <math>\frac{8}{3}</math> seen)</p>
1bi	$x = a + \frac{bv^2}{k}$ $x = 2 + \frac{3(-4)^2}{5} = 11.6$	B1
1bii	$x = a + \frac{bv^2}{k}$ $x - a = \frac{bv^2}{k}$ $k(x - a) = bv^2$ $\frac{k(x - a)}{b} = v^2$ $v = \pm \sqrt{\frac{k(x - a)}{b}}$	<p>M1 (elimination of fraction)</p> <p>M1 (square root)</p> <p>A1 (<math>\pm</math> seen)</p>
1c	$4x + 7y = -23 \text{ ----- (1)}$ $6x - 2y = 3 \text{ ----- (2)}$ $(1) \times 3 : 12x + 21y = -69 \text{ ----- (3)}$ $(2) \times 2 : 12x - 4y = 6 \text{ ----- (4)}$ $(3) - (4) : 25y = -75$ $y = -3$ $x = -0.5$	<p>M1 (correct method to eliminate one variable)</p> <p>A1</p> <p>A1</p>
1d	$\frac{x^2 - (x - y)(x + y)}{(x + y)(x - 3y)}$ $= \frac{x^2 - (x^2 - y^2)}{(x + y)(x - 3y)}$ $= \frac{y^2}{(x + y)(x - 3y)}$	<p>M1</p> <p>A1 (accept expanded denominator)</p>

**11 marks**

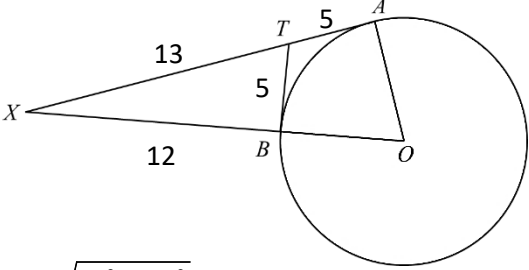
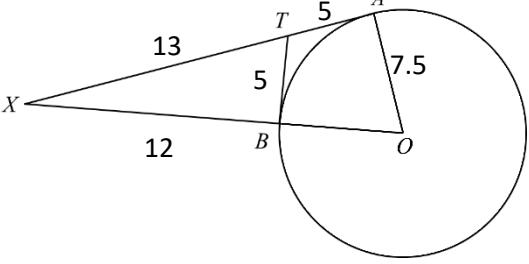
No.	Answers	Marks
2a	$1500 = \frac{25000 \times R \times \frac{9}{12}}{100}$ $R = 8$ Rate is 8%	M1 (or equivalent)  A1
2b	\$1 = 26.77 THB \$500 = 500 x 26.77 = 13385 THB Money left = 13385 – 10600 = 2785 THB  26.88 THB = \$1 $2785 \text{ THB} = \frac{2785}{26.88} = \$103.61$	M1 (get remaining amount of money left in THB)   A1 (nearest cent)
2c	Deposit = $\frac{15}{100} \times 2700 = \$405$ Total instalments = 68 x 36 = \$2448 Total paid = 405 + 2448 = \$2853 Interest = 2853 – 2700 = \$153  $\% \text{ required} = \frac{153}{2700} \times 100 = 5.67\% \quad (5\frac{2}{3}\%)$	M1 (calculate both deposit & instalments)    M1 (their interest $\vee \div$ cash price x 100) A1
2d	100% $\rightarrow$ \$180 110% $\rightarrow \frac{110}{100} \times 180 = \$198$  75% $\rightarrow$ \$198 100% $\rightarrow \frac{100}{75} \times 198 = \$264$	M1 (find discounted price)   M1 ( $\vee$ from above discounted price) A1  <p style="text-align: right;"><b>10 marks</b></p>

No.	Answers	Marks
3a	<p>length of box = <math>3x + 1 - 3 - 3 = (3x - 5)cm</math></p> <p>width of box = <math>x + 13 - 3 - 3 = (x + 7)cm</math></p> <p>height of box = <math>3cm</math></p> <p><i>volume</i> = <math>3(3x - 5)(x + 7)</math></p> <p><math>930 = 3(3x^2 + 21x - 5x - 35)</math></p> <p><math>310 = 3x^2 + 16x - 35</math></p> <p><math>3x^2 + 16x - 345 = 0</math></p>	<p>B1 (Length &amp; width)</p> <p>M1 √</p> <p>M1 (expansion √)</p> <p>A1 (establish the equation)</p>
3b	<p><math>x = \frac{-16 \pm \sqrt{16^2 - 4(3)(-345)}}{2(3)}</math></p> <p><math>x = 8.38</math> or <math>x = -13.72</math></p>	<p>B1</p> <p>B1 B1</p>
3c	<p>Length of box = <math>3(8.38) - 5 = 20.14cm</math></p> <p>Width = <math>8.38 + 7 = 15.38</math> cm</p> <p>Length of SQ = <math>\sqrt{20.14^2 + 15.38^2} = 25.3</math> cm</p>	<p>M1 (√ find either length or width with Q3b value)</p> <p>M1 &amp; A1 √</p> <p><b>10 marks</b></p>

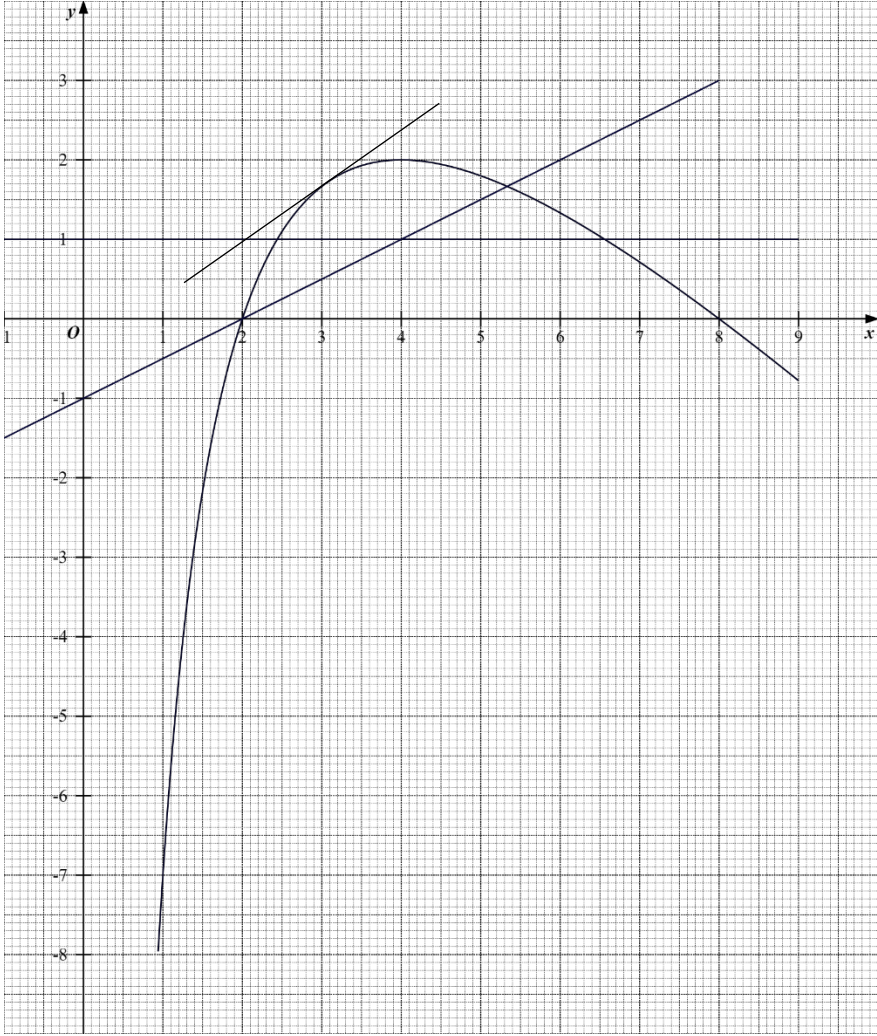
No.	Answers	Marks
4ai	$\overrightarrow{AB} = \overrightarrow{AO} + \overrightarrow{OB}$ $= \begin{pmatrix} -3 \\ -7 \end{pmatrix} + \begin{pmatrix} 13 \\ -8 \end{pmatrix}$ $= \begin{pmatrix} 10 \\ -15 \end{pmatrix}$ $\left  \begin{pmatrix} 10 \\ -15 \end{pmatrix} \right  = \sqrt{10^2 + (-15)^2} = 18.0$	<p>M1 or use length formula</p> <p>A1</p>
4aii	$\overrightarrow{BA} = 2\overrightarrow{AP}$ $\begin{pmatrix} -10 \\ 15 \end{pmatrix} = 2(\overrightarrow{AO} + \overrightarrow{OP})$ $\begin{pmatrix} -5 \\ 7.5 \end{pmatrix} = \begin{pmatrix} -3 \\ -7 \end{pmatrix} + \overrightarrow{OP}$ $\overrightarrow{OP} = \begin{pmatrix} -2 \\ 14.5 \end{pmatrix}$ <p>P (-2, 14.5)</p>	<p>M1</p> <p>A1</p>
4b(i)	$\overrightarrow{CP} = \frac{3}{4}\overrightarrow{CB}$ $= \frac{3}{4}(-4\underline{a} + 2\underline{b})$ $= -3\underline{a} + \frac{3}{2}\underline{b}$	<p>B1 for <math>\overrightarrow{CB}</math></p> <p>B1</p>
4b(ii)	$\overrightarrow{AP} = \overrightarrow{AC} + \overrightarrow{CP}$ $= 2\underline{a} - 3\underline{a} + \frac{3}{2}\underline{b}$ $= -\underline{a} + \frac{3}{2}\underline{b}$	B1
4b(iii)	$\overrightarrow{AD} = -2\underline{a} + 3\underline{b}$ $\overrightarrow{AD} = 2(-\underline{a} + \frac{3}{2}\underline{b})$ $= 2\overrightarrow{AP}$ <p><math>\overrightarrow{AD}</math> is a scalar multiple of <math>\overrightarrow{AP}</math>, AD and AP are parallel with A as the common point.</p> <p><math>\therefore</math> A, D and P lie on the same straight line.</p>	<p>B1 (or find <math>\overrightarrow{PD}</math>)</p> <p>M1 (express one vector as a scalar multiple of the other)</p> <p>A1</p>
4b(iv)	<p>AreaOCB : AreaCBD : AreaCPD</p> <p>2 : 1</p> <p>4 : 3</p> <p>Answer: <math>\frac{8}{3}</math></p>	<p>B1</p> <p><b>11 marks</b></p>

No.	Answers	Marks
5a	 <p>Bearing of B from C = <math>180 - (90 - 33) = 123^\circ</math></p>	M1 A1
5b	$\frac{AB}{\sin(180 - 52 - 33)^\circ} = \frac{43}{\sin 33^\circ}$ $AB = 78.65 = 78.7m(3sf)$	M1 A1
5c	$\cos \angle CDA = \frac{67^2 + 32^2 - 43^2}{2(67)(32)}$ $\angle CDA = 31.297 = 31.3^\circ(1dp)$	M2 A1
5d	$\tan \theta = \frac{60}{67}$ $\theta = 41.84 = 41.8^\circ(1dp)$	M1 A1

9 marks

No.	Answers	Marks
6a	$\angle OAT = \angle OBT = 90^\circ$ (radius $\perp$ tangent) $\therefore \angle OAX = \angle TBX = 90^\circ$ $\angle AXO = \angle BXT$ (common angle) $\angle AOX = \angle BOT$ (3 <sup>rd</sup> angle in triangle) $\therefore \triangle OAX$ and $\triangle OTB$ are similar.	B2 for the first 3 or all statements seen (B1 for one correct pair of angles with reason)
6bi	 $TB = \sqrt{13^2 - 12^2} = 5$ $TA = TB = 5 \text{ cm (tangents from external point)}$ $\frac{OA}{5} = \frac{18}{12}$ $OA = 7.5$	M1 (TB = 5 seen)  M1 (form ratio to find OA oe) A1
6bii	$\frac{\text{area } \triangle TBX}{\text{area } \triangle OAX} = \left(\frac{12}{18}\right)^2 = \frac{4}{9}$ $\frac{\text{area } \triangle TBX}{\text{area quad } OATB} = \frac{4}{5}$	B1 A1
6biii	 $\tan \angle AOX = \frac{18}{7.5}$ $\angle AOX = 67.38^\circ$ $\text{Reflex } \angle AOB = 360 - 67.38 = 292.62^\circ$ $\text{In radian, } \frac{292.62}{180} \times \pi = 5.11 \text{ rad (3sf)}$	M1 (oe for $\angle AOX$ )  M1 (conversion) A1

10 marks

7a	2	B1
7b	<p>Smooth curve through 9 correct points</p> 	<p>B3</p> <p>Or (B2FT for 9 points correct)</p> <p>Or (B1FT for 7 or 8 points correct)</p>
7c	<p>Gradient value between 0.6 to 0.9      [exact value is <math>\frac{7}{9} = 0.\dot{7}</math>]</p>	<p>M1 tangent line at <math>x = 3</math></p> <p>A1</p>
7d	$9 - x - \frac{16}{x} = 0$ $10 - x - \frac{16}{x} = 1$ $y = 1$ $x = [2.3 - 2.5] \text{ or } x = [6.5 - 6.7]$	<p>A1 A1</p>
7e(i)	$10 - x - \frac{16}{x} = mx - 1$ $10x - x^2 - 16 = mx^2 - x$ $mx^2 + x^2 - 11x + 16 = 0$ $(m+1)x^2 - 11x + 16 = 0$	<p>M1 [elimination of fraction]</p> <p>B1</p>
7e(ii)	$\frac{1}{2}$	<p>B1</p> <p><b>11 marks</b></p>

8a(i)	48 g	B1															
8a(ii)	$51 - 45 = 6 \text{ g}$ or $51.5 - 45 = 6.5 \text{ g}$	B1 (for LQ or UQ) A1															
8a(iii)	40 g	B1															
8b	$260 - 200 = 60$ $\frac{60}{300} \times \frac{59}{299} = \frac{59}{1495}$	M1 A1 (accept 0.0395)															
8c(i)	1 <sup>st</sup> batch of eggs: interquartile range = 6 g (6.5g) 2 <sup>nd</sup> batch of eggs: interquartile range = 10 g Since 6 g < 10 g, the mass of the 1 <sup>st</sup> batch varies less widely, hence the mass is more consistent.	B1															
8c(ii)	The mass of the top 25% varies more widely than the bottom 25%.	B1  <b>8 marks</b>															
9a	p = 0.2979 (4 dp) r = 11.03 (2 dp) s = 133.62 (2 dp)	B3 (for each answer)															
9b	July National average electricity usage = 505 kWh Current July usage = 289 kWh Additional usage = 505 – 289 = 216 kWh Additional amount = 216 x 0.2979 (rate) = \$64.3464 = \$64.35  Monthly cost (from air-con) must be < \$64.35 } <i>4 &amp; 5 ticks model selected</i>  <table> <thead> <tr> <th><u>Model</u></th><th><u>monthly cost (\$)</u></th><th><u>LCC (\$)</u></th></tr> </thead> <tbody> <tr> <td>B</td><td>616 ÷ 12 = <b>51.33</b></td><td>2749 + 616 x 7 = <b>7061</b></td></tr> <tr> <td>C</td><td>789 ÷ 12 = 65.75</td><td>1989 + 789 x 7 = 7512</td></tr> <tr> <td>D</td><td>552 ÷ 12 = <b>46</b></td><td>3499 + 552 x 7 = <b>7363</b></td></tr> <tr> <td>E</td><td>594 ÷ 12 = <b>49.50</b></td><td>3305 + 594 x 7 = 7463</td></tr> </tbody> </table> Chen should opt for Model D which has the lowest monthly cost (< \$64.35) and the LCC is the second lowest among the four models.  Estimated August bill = 1.09 x (122.59 + 46) = \$183.76	<u>Model</u>	<u>monthly cost (\$)</u>	<u>LCC (\$)</u>	B	616 ÷ 12 = <b>51.33</b>	2749 + 616 x 7 = <b>7061</b>	C	789 ÷ 12 = 65.75	1989 + 789 x 7 = 7512	D	552 ÷ 12 = <b>46</b>	3499 + 552 x 7 = <b>7363</b>	E	594 ÷ 12 = <b>49.50</b>	3305 + 594 x 7 = 7463	M1 M1 M1  M1 (monthly cost) M1 (LCC) Calculated for BCDE or DE  A1  A1   <b>10 marks</b>
<u>Model</u>	<u>monthly cost (\$)</u>	<u>LCC (\$)</u>															
B	616 ÷ 12 = <b>51.33</b>	2749 + 616 x 7 = <b>7061</b>															
C	789 ÷ 12 = 65.75	1989 + 789 x 7 = 7512															
D	552 ÷ 12 = <b>46</b>	3499 + 552 x 7 = <b>7363</b>															
E	594 ÷ 12 = <b>49.50</b>	3305 + 594 x 7 = 7463															