

Broadrick Secondary School

4E5N Preliminary Examination 2024

Paper 2 Marking Scheme

1a	$4.2 \times 10^6$	B1
b	$\frac{4.2 \times 10^6 - 3.6 \times 10^6}{3.6 \times 10^6} \times 100\%$ $= 16\frac{2}{3}\%$	M1 A1
c	$\frac{3.6 \times 10^6}{100 - 4} \times 100\%$ $= 3750000$ $= 3.75 \times 10^6$	M1 A1
2a	$12x - 8x^2 = 6 - 8x^2$ $12x = 6$ $x = \frac{1}{2}$	M1 A1
b	$1 - 3p \geq 5$ $-3p \geq 4$ $p \leq -\frac{4}{3}$	B1
c	$3A = \frac{Ap + h}{1 - h}$ $3A(1 - h) = Ap + h$ $3A - 3Ah = Ap + h$ $3A - 3Ah - Ap = h$ $A(3 - 3h - p) = h$ $A = \frac{h}{3 - 3h - p}$	M1 (make linear) M1 (Factorise) A1
d		M1 (combine) M1 (expand)

	$\frac{x}{(x-4)^2} - \frac{3}{4-x} = 2$ $\frac{x}{(x-4)^2} + \frac{3}{x-4} = 2$ $\frac{x+3(x-4)}{(x-4)^2} = 2$ $x+3x-12 = 2(x^2-8x+16)$ $4x-12 = 2x^2-16x+32$ $0 = 2x^2-20x+44$ $0 = x^2-10x+22$ $x = \frac{-(-10) \pm \sqrt{(-10)^2 - 4(1)(22)}}{2(1)}$ $= \frac{10 \pm \sqrt{12}}{2}$ $= 6.73 \text{ or } 3.27 \text{ (2dp)}$	<p>M1 (quadratic formula using their found eqn)</p> <p>A1</p>
3a	$3y+5x-6=0$ $y = -\frac{5}{3}x+2$ $-1 = -\frac{5}{3}(-3)+c$ $c = -6$ $y = -\frac{5}{3}x-6$	<p>M1 (find m)</p> <p>M1</p> <p>A1</p>
b	$y = -\frac{5}{3}(0)-6 = -6$ $B(0,-6)$ $\text{Mid point of BD} = (0, \frac{9+(-6)}{2}) = (0, 1.5)$ <p>C is (x, 1.5) and sub into <math>y = 7.5 - x</math></p> $1.5 = 7.5 - x$ $x = 6$ <p>So C is (6, 1.5)</p>	<p>M1 (find y value of C)</p> <p>A1</p>
c	$\text{Area} = \frac{1}{2}(15)(3) + \frac{1}{2}(15)(6)$	<p>M1</p> <p>A1 (ECF from</p>

	=67.5	(b))
d	<p>Let <math>P</math> be <math>(0, -1)</math>.</p> $\tan \angle ABP = \frac{3}{5}$ $\angle ABP = \tan^{-1}\left(\frac{3}{5}\right)$ <p>Let <math>Q</math> be <math>(0, 1.5)</math>.</p> $\tan \angle CBQ = \frac{6}{7.5}$ $\angle CBQ = \tan^{-1}\left(\frac{6}{7.5}\right)$ $\angle ABC = \tan^{-1}\left(\frac{3}{5}\right) + \tan^{-1}\left(\frac{6}{7.5}\right)$ $= 69.6^\circ$ <p>Or find length of AB, BC and AC and use cosine rule.</p>	<p>M1</p> <p>M1</p> <p>A1</p>
4a	20	B1
bi	<p><math>X = pn^2 + qn</math></p> <p>When <math>n = 4</math> and <math>X=2</math>,</p> $2 = p(4)^2 + q(4)$ $2 = 16p + 4q$ <p>When <math>n = 5</math> and <math>X=5</math>,</p> $5 = p(5)^2 + q(5)$ $5 = 25p + 5q$	<p>A1</p> <p>A1</p>
bii	$16p + 4q = 2$ $80p + 20q = 10 \text{ --- (1)}$ $25p + 5q = 5$ $100p + 20q = 20 \text{ --- (2)}$ $(2) - (1)$ $20p = 10$ $p = 0.5$ $q = -1.5$	<p>M1</p> <p>A1</p> <p>A1</p>
biii		M1

	$495 = 0.5n^2 - 1.5n$ $0 = -495 - 1.5n + 0.5n^2$ $0 = n^2 - 3n - 990$ $(n - 33)(n + 30) = 0$ $n = 33 \quad \text{or} \quad n = -30 \text{ (rej)}$  Since number of vertices is an integer, it is possible to have a $n$ -sided polygon with 495 diagonals.	M1  A1
5ai	$\angle ABC = \frac{100}{2} = 50^\circ$ <i>(angle at centre = 2x angle at circumference)</i>	B1
aii	$\angle ADC = 180^\circ - 50^\circ = 130^\circ$ <i>(angles in opp seg)</i>	B1
aiii	$\angle ACO = \frac{180^\circ - 100^\circ}{2} = 40^\circ$ <i>(base angles of isos triangle)</i> $\angle COT = 40^\circ$ <i>(alt angles, AC//OT)</i> $\angle OCT = 90^\circ$ <i>(tan perpendicular to rad)</i> $\angle OTC = 180^\circ - 90^\circ - 40^\circ = 50^\circ$ <i>(angle sum of triangle)</i>	M1  M1 A1
b	$\angle ADC + \angle AOC = 130^\circ + 100^\circ$ $= 230^\circ$ $\neq 180^\circ$  They are not angles in opposite segment. A circle cannot be drawn passing through the points $A$ , $O$ , $C$ and $D$ .	B1
c	$\tan 50^\circ = \frac{OC}{4.8}$ $OC = 5.72042$  Minor segment = minor sector – triangle $= \frac{100}{360} \times \pi (5.72042)^2 - \frac{1}{2} (5.72042)^2 \sin(100^\circ)$ $= 12.4 \text{ cm}^2$	M1  M1 A1
6a	-3.33 (2dp)	B1
6b	All points plotted correctly Smooth curve	P2 C1
6ci	Tangent drawn such that it passes through (-1,2) and touches curve at 1 point and gradient is negative.	C1
6cii	$m = \frac{2 - (-1)}{-1 - 0} = -3$ $c = -1$ $y = -3x - 1$	M1  A1
6d		

	$\frac{1}{x-1} - \frac{1}{4}x = 0$ $\frac{1}{x-1} - \frac{1}{4}x + \frac{5}{4}x - 1 = \frac{5}{4}x - 1$ $y = \frac{5}{4}x - 1$ <p>Draw line on graph</p> <p><math>x = \underline{2.6}</math> and <math>\underline{-1.5}</math>          (accept 2.5, 2.55) (accept -1.4, -1.45, -1.55, -1.6)</p>	<p>M1</p> <p>M1</p> <p>A1</p>
7ai	Median = 353 g	B1
aii	UQ: 366 or 367 LQ: 342 or 343 IQR = 366 – 342 = 24g (also accept 23 or 25 g depending on their UQ & LQ)	<p>M1</p> <p>A1</p>
b	20%-->32 apples  Read at 128 <sup>th</sup> apple Min mass = 370 g	<p>M1</p> <p>A1</p>
c	$\frac{14}{160} \times \frac{160-104}{159} \times 2$ $= 0.0616$	<p>M1</p> <p>A1</p>
d	False. The first quartile which represents 25% of the apples are less than 320g. The upper quartile which represents 75% of the apples are less than 360g which implies that 25% of the apples are more than 360g  Hence there are equal number of apples weighing less than 320g and more than 360g.	<p>B1 (states that the whiskers rep 25% of the data)</p>
e	I disagree.  The median mass of apples from tree A is the same as that from tree B. On average, apples from tree A and B weigh the same.  IQR (Tree B) = 360 – 320 = 40g However, the interquartile range of the masses of the apples from tree B is bigger than that from tree A. The masses of the apples from tree B have a bigger spread, thus are less consistent.	<p>B1</p> <p>B1</p>

8a	$BE = \sqrt{15^2 + 8^2}$ $= 17 \text{ cm}$	M1 A1
b	$AG = \sqrt{17^2 + 10^2} = \sqrt{389}$ $= 19.7 \text{ cm (3sf)}$	M1 A1
c	<p>Let <math>M</math> be the midpoint of <math>CG</math> and <math>N</math> be the midpoint of <math>BF</math>.</p> $JM = \sqrt{8^2 - 4^2} = \sqrt{48}$ <p>Then <math>JN = 10 + \sqrt{48}</math></p> $AN = \sqrt{15^2 + 4^2} = \sqrt{241}$ $AJ^2 = (\sqrt{241})^2 + (10 + \sqrt{48})^2$ $AJ = 22.96876$ $= 22.97 \text{ (4sf) (shown)}$	M1 M1  M1  A1
d	$\cos \angle JAG = \frac{22.97^2 + (\sqrt{389})^2 - 8^2}{2 \times 22.97 \times \sqrt{389}}$ $\angle JAG = 19.7796 = 19.8^\circ \text{ (1dp)}$ <p>If use exact value, angle = <math>19.78165 = 19.8^\circ \text{ (1dp)}</math></p>	M1  A1
9a	$\text{Capacity} = \frac{1}{3}\pi(2)^2(3) + \frac{2}{3}\pi(3)^3$ $= 69.1150 = 69.1 \text{ m}^3$	M1 A1
b	<p>Curved hemisphere = <math>2\pi(3)^2 = 18\pi</math></p> <p>Ring = <math>\pi(3)^2 - \pi(2)^2 = 5\pi</math></p> <p>Slant height of cone, <math>L = \sqrt{2^2 + 3^2} = \sqrt{13}</math></p> <p>Curved area of big cone = <math>\pi(2)\sqrt{13} = 2\pi\sqrt{13}</math></p> <p>Using similar solids,</p> $\frac{h_{\text{small cone}}}{h_{\text{big cone}}} = \sqrt[3]{\frac{1}{10}}$ $\frac{A_{\text{small cone}}}{A_{\text{big cone}}} = \left(\sqrt[3]{\frac{1}{10}}\right)^2 = \frac{1}{\sqrt[3]{100}}$ $\frac{A_{\text{contact with water}}}{A_{\text{big cone}}} = \frac{\sqrt[3]{100} - 1}{\sqrt[3]{100}}$ $A_{\text{contact with water}} = \frac{\sqrt[3]{100} - 1}{\sqrt[3]{100}} \times 2\pi\sqrt{13} = 17.7736$ <p>Total area in contact = <math>18\pi + 5\pi + 17.7736</math></p>	M1 (Hemisphere or ring)  M1 (CSA of big cone using their L)   M1 (find ratio of h and then area)    M1 (find area of cone in contact)

	$= 90.0302 = 90.0 \text{ m}^2$	A1																														
10a	$\frac{300}{1200} \times 100\% = 25\%$	B1																														
b	$6 + 1.8 \times 2 \times 49 = \$182.40$	M1, A1																														
c	<table border="1"> <thead> <tr> <th>Item</th><th>Description</th><th>Total cost</th></tr> </thead> <tbody> <tr> <td>Printing of T-shirts</td><td>Double side (Bundle of 500 pcs)</td><td><math>\\$7000 \times 2 = \\$14000</math></td></tr> <tr> <td>Goodie Bags</td><td>No of packs req = <math>1000/5 = 200</math>  Bulk price (100+ packs)</td><td><math>\\$18 \times 200 = \\$3600</math></td></tr> <tr> <td>Booking of venue</td><td>6 months in advance</td><td><math>\\$1200</math></td></tr> <tr> <td>Refreshments</td><td>Large set  Regular set  Small set</td><td><math>\\$3 \times 1000 = \\$3000</math> or <math>\\$2.80 \times 1000 = \\$2800</math> or <math>\\$2.50 \times 1000 = \\$2500</math></td></tr> <tr> <td>Participants medals</td><td>Number of pack of 50 = <math>1000/50 = 20</math></td><td><math>\\$210 \times 20 = \\$4200</math></td></tr> </tbody> </table> <p>Total weight of shirts = <math>140 \text{ g} \times 1000 = 140 \text{ kg}</math></p> <table border="1"> <thead> <tr> <th>Local Courier</th><th>Number of parcels</th><th>Cost</th></tr> </thead> <tbody> <tr> <td>Simply Post</td><td><math>\frac{140}{80} \approx 2</math> 1 parcel of 80 kg + 1 parcel of 60 kg</td><td><math>(4.80 + 1.85 \times 2 \times 79)</math> <math>+(4.80 + 1.85 \times 2 \times 59)</math> <math>= 520.20</math></td></tr> <tr> <td>Singapore Post</td><td><math>\frac{140}{50} \approx 3</math> 2 parcels of 50 kg + 1 parcel of 40 kg</td><td><math>2(6 + 1.80 \times 2 \times 49)</math> <math>+(6 + 1.80 \times 2 \times 39)</math> <math>= 511.20</math></td></tr> <tr> <td>DPEX</td><td><math>\frac{140}{30} \approx 5</math> 4 parcels of 30 kg + 1 parcel of 20 kg</td><td><math>4(5.5 + 1.60 \times 2 \times 29)</math> <math>+(5.5 + 1.60 \times 2 \times 19)</math> <math>= 727.60</math></td></tr> </tbody> </table> <p><i>Choose Singapore Post &amp; Large Set of refreshment.</i></p> <p>Total costs after GST =</p> $(14000 + 3600 + 1200 + 3000 + 4200 + 511.20) \times \frac{109}{100}$	Item	Description	Total cost	Printing of T-shirts	Double side (Bundle of 500 pcs)	$\$7000 \times 2 = \$14000$	Goodie Bags	No of packs req = $1000/5 = 200$  Bulk price (100+ packs)	$\$18 \times 200 = \$3600$	Booking of venue	6 months in advance	$\$1200$	Refreshments	Large set  Regular set  Small set	$\$3 \times 1000 = \$3000$ or $\$2.80 \times 1000 = \$2800$ or $\$2.50 \times 1000 = \$2500$	Participants medals	Number of pack of 50 = $1000/50 = 20$	$\$210 \times 20 = \$4200$	Local Courier	Number of parcels	Cost	Simply Post	$\frac{140}{80} \approx 2$ 1 parcel of 80 kg + 1 parcel of 60 kg	$(4.80 + 1.85 \times 2 \times 79)$ $+(4.80 + 1.85 \times 2 \times 59)$ $= 520.20$	Singapore Post	$\frac{140}{50} \approx 3$ 2 parcels of 50 kg + 1 parcel of 40 kg	$2(6 + 1.80 \times 2 \times 49)$ $+(6 + 1.80 \times 2 \times 39)$ $= 511.20$	DPEX	$\frac{140}{30} \approx 5$ 4 parcels of 30 kg + 1 parcel of 20 kg	$4(5.5 + 1.60 \times 2 \times 29)$ $+(5.5 + 1.60 \times 2 \times 19)$ $= 727.60$	<p>M1 (T-shirt printing)</p> <p>M1 (bag)</p> <p>M1 (medals)</p> <p>M1 (shipping)</p> <p>M1 (cost after GST)</p>
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	<p>=28897.208</p> <p>At least 40% to charity, so 60% will be to cover costs:</p> <p>Including charity = <math>28897.208 \times \frac{100}{60} = 48162.01</math></p> <p>Fee for each participant = <math>\frac{48162.01}{1000} = \\$48.16</math></p> <p>To donate at least 60% of the proceeds and cover all costs, sensible amount to charge each participant = \$50.</p>	<p>M1 (total including charity)</p> <p>A1</p>
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